Introduction

- Though debates on quantum nature of black holes are crucial and long standing, there is no systematic study by quantum gravity so far to lav a solid theoretical foundation for arguments
- > Some different models of quantum gravity are effective ways to understand gravity behaviors at a sufficiently small scale: String theory, Loop quantum gravity, Asymptotically safe gravity, Noncommutative gravity, Quadratic gravity, Rainbow gravity,
- Several aspects of quantum black holes have been discussed namics, Hawking radiation, Quasinormal modes, Stabilities, Accretion disk, Periapsis shift, Gravitational time delay, Light deflection, Gravitational Jensing, Black hole shadow,

Loop quantum corrected black holes

 $ds^2 = -f(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\Omega^2, \ f(r) = 1 - \frac{2GM}{r} + \frac{\alpha G^2 M^2}{r^4}$

 $\begin{bmatrix} \mathbf{0} < \beta < \mathbf{1}/2 : M < M_{\min} := \frac{4\sqrt{3\alpha}}{9G} : \text{No horizon} \\ \mathbf{1}/2 < \beta < \mathbf{1} : M > M_{\min} : \text{two Killing horizons} \\ r_{\pm} = \frac{M(1+\beta)\left(1 \pm \sqrt{2\beta-1}\right)}{2\beta} \end{bmatrix}$

✓ Inner horizon r_ is unstable with respect to scalar perturbations

Modified thermodynamics

• <u>Temperature</u>: $T = \frac{\kappa}{\alpha} = \frac{(r_+ - r_-)(r_+^2 + (r_+ + r_- - 2M)r_+ + \alpha M^2 / (r_+ r_-))}{4}$

 M/m_p

 $(n \text{ with } a \neq 0 \text{ diverges})$

Snarsity is enhanced

by quantum gravity

at $M = M_{\min}$.

effect

25656

ЬſМ

 $\sqrt{\Delta s}$ black hole mass decreases temperature with $\alpha \neq 0$ reaches

local maximum value and then decreases to zero at minimum

Modified sparsity of Hawking radiation

Similar to black hole evaporations in noncommutative model and

asymptotically safe gravity, loop quantum corrected black hole

final stage of evaporation, and then turn into remnant when

Weak gravitational deflection angle of photon

 \checkmark Deflection angle decreases with increasing α/M^2 for fixed b/M.

 $128M^3 \left(28M^2 - \alpha\right) + 1155\pi M^4 \left(221M^2 - 12\alpha\right)$

 $\delta\phi \simeq \frac{4M}{b} + \frac{15\pi M^2}{4b^2} + \frac{128M^3}{3b^3} + \frac{15\pi M^2 \left(231M^2 - 4\alpha\right)}{64b^4}$

would take an infinite amount of time to radiate a particle at

and will probably turn into a null singularity [Cao et al.].

0.020

T 0.015 m_{p 0.010}

0.00

 η 300

value of mass $M_{\min} = 4\sqrt{3\alpha}m_p/(9l_p)$.

 $\alpha = 0$

 $M/m_{\rm m}$

black hole mass M approaches mass M

• Metric is determined for $r \ge r_b = \left(\frac{\alpha GM}{2}\right)^2$

 \Leftrightarrow Dust surface radius $a(\tau)\tilde{r}_0$ runs over $[r_{br} \infty)$

• Introducing parameter $0 < \beta < 1$ by $G^2 M^2 = \frac{4\beta^4}{(1-\beta^2)^3} a$

Gluing interior geometry ds²_{APS} with exterior spherically symmetric one:

Black hole thermodynamics and light deflection

in effective loop quantum gravity

Ken Matsuno

(Osaka Metropolitan University)

$$ds^{2} = -f(r)dt^{2} + \frac{dr^{2}}{f(r)} + r^{2}d\Omega^{2}$$

along radial freefall geodesics by identification $(\tau, \tilde{r}, \theta, \phi) \sim (t(\tau), r(\tau), \theta, \phi)$ such that induced metric and extrinsic curvature are equal on gluing surfaces that become a single C1 surface of dusty part of spacetime

$$f(r) = 1 - \frac{2GM}{r} + \frac{\alpha G^2 M^2}{r^4}$$
A quantum deformation of Schwarzschild spacetime

as derived in effective loop quantum gravity [Kelly et al.]

> A Killing observer perceives energy density:

$$T^q_{\mu\nu} = \frac{G_{\mu\nu}}{8\pi G}, \quad \rho^q = \frac{3\alpha GM^2}{8\pi r^6}$$
 : dark matter candidate

Tunneling of scalar particles

Action for outgoing and ingoing modes for classically forbidden trajectory: $\pi\omega r_{+}^{4}$ $\mathrm{Im}R_{\mathrm{out}} = -\mathrm{Im}R_{\mathrm{in}} = \frac{1}{\left(r_{+} - r_{-}\right)\left(r_{+}^{2} + \left(r_{+} + r_{-} - 2M\right)r_{+} + \alpha M^{2} \left/ \left(r_{+} + r_{-}\right)\right)\right)}$

➤ Tunneling probability amplitude of scalar particles:

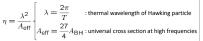
 $\Gamma \simeq \frac{\exp\left(-2ImR_{out}\right)}{\exp\left(-2ImR_{in}\right)} \simeq \exp\left(-\frac{4\pi r_{+}^{4}}{\left(r_{+}-r_{-}\right)\left(r_{+}^{2}+\left(r_{+}+r_{-}-2M\right)r_{+}+\alpha M^{2}\left/\left(r_{+}r_{-}\right)\right)}\right)^{2}$

> Comparing tunneling probability amplitude with Boltzmann factor $\Gamma = \exp(-\omega/T)$ at temperature *T*, we obtain modified Hawking temperature of loop quantum corrected black hole:

$$\begin{split} T &= \frac{\left(r_{+} - r_{-}\right)\left(r_{+}^{2} + \left(r_{+} + r_{-} - 2M\right)r_{+} + \alpha M^{2} / \left(r_{+}r_{-}\right)\right)}{4\pi r_{+}^{4}} \\ &= \frac{\beta \left(1 - 4\beta^{2} - \left(1 - 3\beta - \beta^{2}\right)\sqrt{2\beta - 1}\right)}{\pi M \left(1 - \beta^{2}\right)^{2}}, \quad \beta = \beta(M, \alpha) \end{split}$$

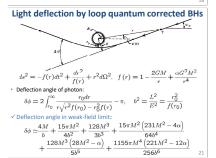
Sparsity of Hawking radiation during BH evaporation

· Sparsity: average time gap between two successive particle emissions over characteristic timescale of individual particle emission



 η≪1 : Hawking radiation is a typical blackbody radiation where its thermal wavelength is much shorter than emitting body size

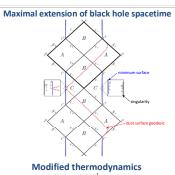
 n≫1 : Hawking radiation is not a continuous emission of particles but a sparse radiation, i.e., most particles are randomly emitted in a discrete manner with pauses in between. ex) $\eta_{4D \text{ Sch.}} = 64\pi^3/27$

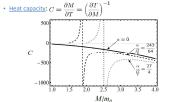




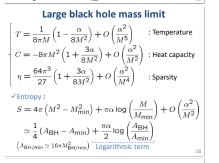
- Thermodynamics of quantum corrected polymer black hole and asymptotically safe gravity black hole have been discussed [Mele et al Mandal Gangonadhyay]
- ✓ These spacetimes admit extremal minimal-sized configurations of quantum gravitational nature characterized by vanishing temperature and entropy
- · Quantum gravity effects on black hole shadows in loop quantum Oppenheimer-Snyder gravitational collapse model have been discussed [Yang et al.]

✓ We study thermodynamics and light deflection of static black holes in loop quantum Oppenheimer-Snyder model as one of quantum gravity effects in Hawking radiation and gravitational lensing, respectively.

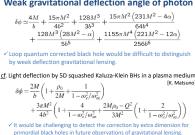


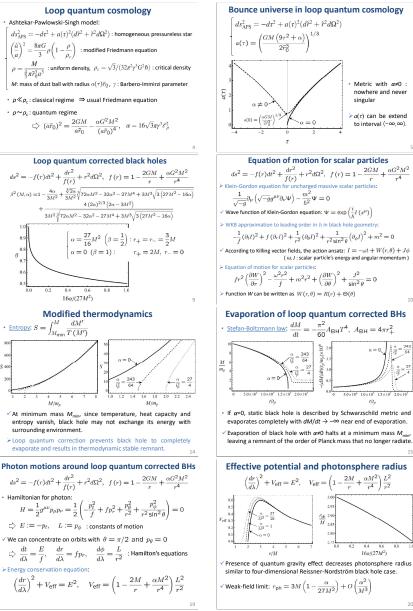


✓ At local maximum temperature, system with α≠0 undergoes transition from unstable negative heat capacity phase to stable positive heat capacity cooling down towards cold extremal configuration with mass Mmin



Weak gravitational deflection angle of photon





We consider thermodynamics and light deflection of 4D static spherically symmetric black holes in quantum Oppenheimer-Snyder model in loop quantum gravity.

Summarv

We derive modified Hawking temperature, heat capacity, entropy, evaporation time, radiation sparsity and weak deflection angle of photon in loop quantum corrected black hole spacetime.

Loop quantum correction may slow down increase of Hawking temperature due to radiation and result in thermodynamic stable remnant

Modified sparsity of Hawking radiation may become infinite when mass of loop quantum corrected black hole approaches its remnant mass

Loop quantum corrected black hole would be difficult to distinguish by weak deflection gravitational lensing

Discussion

- If Barbero-Immirzi parameter is γ=0.24, mass of black hole remnant is $M_{\rm min} = 10^{-8}$ kg, which is of order Planck mass like black hole remnants in minimally geometric deformation model, quadratic gravity and asymptotically safe gravity.
- Since such a black hole remnant would not radiate and its gravitational interaction would be very weak, it would be difficult to observe remnants in our Universe directly

It would be expected that one possible indirect signature of black hole remnant might be associated with cosmic gravitational wave background [Chen. Adler]